

## Appendix

The seven simultaneous algebraic equations for the coefficients

$$\begin{bmatrix} C_{11} & C_{12} & C_{13} & C_{14} & C_{15} & C_{16} & C_{17} \\ C_{21} & C_{22} & C_{23} & C_{24} & C_{25} & C_{26} & C_{27} \\ C_{31} & C_{32} & C_{33} & C_{34} & C_{35} & C_{36} & C_{37} \\ C_{41} & C_{42} & C_{43} & C_{44} & C_{45} & C_{46} & C_{47} \\ C_{51} & C_{52} & C_{53} & C_{54} & C_{55} & C_{56} & C_{57} \\ C_{61} & C_{62} & C_{63} & C_{64} & C_{65} & C_{66} & C_{67} \\ C_{71} & C_{72} & C_{73} & C_{74} & C_{75} & C_{76} & C_{77} \end{bmatrix} \begin{pmatrix} a_1 \\ a_2 \\ a_3 \\ a_4 \\ a_5 \\ a_6 \\ a_7 \end{pmatrix} = \begin{pmatrix} P_1 \\ P_2 \\ P_3 \\ P_4 \\ P_5 \\ P_6 \\ P_7 \end{pmatrix} \quad (A1)$$

where,

$$\begin{aligned} C_{11} &= \frac{131072bD_{11}}{1575a^3} + \frac{524288D_{12}}{11025ab} + \frac{131072aD_{22}}{1575b^3} + \frac{1048576D_{66}}{11025ab} - \frac{65536bN_{xa}}{33075a}, \\ C_{12} &= \frac{131072bD_{11}}{11025a^3} + \frac{131072aD_{22}}{17325b^3}, \\ C_{13} &= \frac{131072bD_{11}}{17325a^3} + \frac{131072aD_{22}}{11025b^3} - \frac{65536bN_{xa}}{363825a}, \\ C_{14} &= \frac{131072bD_{11}}{33075a^3} - \frac{524288D_{12}}{363825ab} + \frac{131072aD_{22}}{75075b^3} - \frac{1048576D_{66}}{363825ab} + \frac{65536bN_{xa}}{1091475a}, \\ C_{15} &= \frac{131072bD_{11}}{75075a^3} - \frac{524288D_{12}}{363825ab} + \frac{131072aD_{22}}{33075b^3} - \frac{1048576D_{66}}{363825ab} - \frac{65536bN_{xa}}{1576575a}, \\ C_{16} &= \frac{65536bD_{11}}{11025a^2} + \frac{65536D_{12}}{33075b} + \frac{131072D_{66}}{33075a}, \\ C_{17} &= \frac{65536D_{12}}{33075a} + \frac{65536aD_{22}}{11025b^2} + \frac{131072D_{66}}{33075a}, \\ C_{21} &= C_{12}, C_{22} = \frac{131072bD_{11}}{3675a^3} + \frac{524288D_{12}}{121275ab} + \frac{131072aD_{22}}{75075b^3} + \frac{1048576D_{66}}{121275ab} - \frac{65536bN_{xa}}{363825a}, \\ C_{23} &= \frac{131072bD_{11}}{121275a^3} + \frac{131072aD_{22}}{121275b^3}, \\ C_{24} &= \frac{6946816bD_{11}}{363825a^3} + \frac{1048576D_{12}}{675675ab} + \frac{131072aD_{22}}{225225b^3} + \frac{2097152D_{66}}{675675ab} - \frac{131072bN_{xa}}{2027025a}, \\ C_{25} &= \frac{131072bD_{11}}{525525a^3} + \frac{131072aD_{22}}{363825b^3}, \\ C_{26} &= -\frac{65536bD_{11}}{33075a^2} - \frac{65536D_{12}}{363825b} - \frac{131072D_{66}}{363825b}, \\ C_{27} &= \frac{65536aD_{22}}{121275b^2}, \\ C_{31} &= C_{13}, C_{32} = C_{23}, \\ C_{33} &= \frac{131072bD_{11}}{75075a^3} + \frac{524288D_{12}}{121275ab} + \frac{131072aD_{22}}{3675b^3} + \frac{1048576D_{66}}{121275ab} - \frac{65536bN_{xa}}{1576575a}, \\ C_{34} &= \frac{131072bD_{11}}{363825a^3} + \frac{131072aD_{22}}{525525b^3} + \frac{65536bN_{xa}}{12006225a}, \\ C_{35} &= \frac{131072bD_{11}}{225225a^3} + \frac{1048576D_{12}}{675675ab} + \frac{6946816aD_{22}}{363825b^3} + \frac{2097152D_{66}}{675675ab} - \frac{65536bN_{xa}}{4729725a}, \\ C_{36} &= \frac{65536bD_{11}}{121275a^2}, \\ C_{37} &= -\frac{65536D_{12}}{363825a} - \frac{65536aD_{22}}{33075b^2} - \frac{131072D_{66}}{363825a}, \\ C_{41} &= C_{14}, C_{42} = C_{24}, C_{43} = C_{34}, \\ C_{44} &= \frac{84279296bD_{11}}{4729725a^3} + \frac{524288D_{12}}{525525ab} + \frac{131072aD_{22}}{546975b^3} + \frac{1048576D_{66}}{525525ab} - \frac{65536bN_{xa}}{1576575a}, \\ C_{45} &= \frac{131072bD_{11}}{1576575a^3} + \frac{524288D_{12}}{12006225ab} + \frac{131072aD_{22}}{1576575b^3} + \frac{1048576D_{66}}{12006225ab} + \frac{65536bN_{xa}}{52026975a}, \\ C_{46} &= -\frac{65536bD_{11}}{51975a^2} - \frac{65536D_{12}}{525525b} - \frac{131072D_{66}}{525525b}, \\ C_{47} &= -\frac{65536D_{12}}{1091475a} + \frac{65536aD_{22}}{525525b^2} - \frac{131072D_{66}}{1091475a}, \\ C_{51} &= C_{15}, C_{52} = C_{25}, C_{53} = C_{35}, C_{54} = C_{45}, \\ C_{55} &= \frac{131072bD_{11}}{546975a^3} + \frac{524288D_{12}}{525525ab} + \frac{84279296aD_{22}}{4729725b^3} + \frac{1048576D_{66}}{525525ab} - \frac{65536bN_{xa}}{11486475a}, \\ C_{56} &= \frac{65536bD_{11}}{525525a^2} - \frac{65536D_{12}}{1091475b} - \frac{131072D_{66}}{1091475b}, \\ C_{57} &= -\frac{65536D_{12}}{525525a} - \frac{65536aD_{22}}{51975b^2} - \frac{131072D_{66}}{525525a}, \\ C_{61} &= C_{16}, C_{62} = C_{26}, C_{63} = C_{36}, C_{64} = C_{46}, C_{65} = C_{56}, \\ C_{66} &= \frac{16384abA_{55}}{1091475} + \frac{65536bD_{11}}{99225a} + \frac{65536aD_{66}}{363825b}, \\ C_{67} &= \frac{16384D_{12}}{99225} + \frac{16384D_{66}}{99225}, \\ C_{71} &= C_{17}, C_{72} = C_{27}, C_{73} = C_{37}, C_{74} = C_{47}, C_{75} = C_{57}, C_{76} = C_{67}, \\ C_{77} &= \frac{16384abA_{44}}{1091475} + \frac{65536aD_{22}}{99225b} + \frac{65536bD_{66}}{363825a}, \\ P_1 &= -\frac{64abp}{225}, \\ P_2 &= P_3 = -\frac{64abp}{1575}, \\ P_4 &= P_5 = -\frac{64abp}{4725}, \\ P_6 &= P_7 = 0 \end{aligned}$$